

EXPLORING DYON CONDENSATION AND DUAL SUPERCONDUCTIVITY WITHIN THE ABELIAN HIGGS MODEL OF QUANTUM CHROMODYNAMICS (QCD)

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Abstract

The ideas of dyon condensation and dual superconductivity are investigated within the framework of the Abelian Higgs model of quantum gravity (QCD). By analyzing these events, we can better understand the complicated dynamics of QCD at extreme conditions, such high density and high temperatures. A dyon's electrical or magnetic charge can screen its own direct potential—to which it minimally couples—and ant screening the dual potential—in compliance with the generalized Meissner effect—leading to dual superconductivity, as shown by the construction of the effective action for dyonic field in Abelian projection of QCD. The average Wilson loop representation of a dual superconductivity and confinement Abelian Higgs model has been achieved by the Abelian projection of QCD. Theoretical and experimental physicists in disciplines as diverse as particle physics and cosmology stand to benefit from a better understanding of these features, which advances our understanding of basic particles and their interactions.

Keywords: *Dyon, Condensation, Dual Superconductivity, Abelian, Higgs Model, Quantum Chromodynamics (QCD)*

1.INTRODUCTION

Within the framework of the Abelian Higgs model of QCD, the study of dyon condensation and dual superconductivity is a fascinating area of theoretical physics. The fundamental theory of quantum chromodynamics describes the strong force that controls the interactions between quarks, which are the constituents of protons, neutrons, and other hadrons. Although QCD is remarkably successful in explaining the dynamics of quarks and gluons at high energies, understanding their dynamics in harsh environments—such as the early cosmos or dense astrophysical objects like neutron stars—remains a daunting challenge. Simplified models that capture key aspects of QCD and allow for theoretical analysis are frequently used by physicists to address these issues. A model that resembles the Higgs field in the Standard Model of particle physics is the Abelian Higgs model, which mixes scalar fields and gauge fields, which stand in for the gluons in QCD. This model offers a foundation for investigating QCD's nonperturbative events, revealing details about the mechanisms governing confinement, magnetic monopole production, and other fascinating phenomena.

In the context of the Abelian Higgs model, dyon condensation is the spontaneous production of dyons, which are charged particles that possess both electric and magnetic properties. In addition to providing a possible explanation for events like confinement, in which quarks and gluons are permanently trapped within color-neutral hadrons, these composite particles are essential in clarifying the nonperturbative dynamics of QCD. Scientists want to shed insight on the underlying nature of the strong force by deciphering the enigmas surrounding confinement and the creation of topological defects such as magnetic monopoles through the study of dyon condensation. Analogously, the idea of dual superconductivity in the Abelian Higgs model offers important new perspectives on QCD behavior in extreme conditions. Some gauge theories in dual superconductivity have superconductor-like properties, but in a dual space. This duality suggests that quarks and gluons can be contained within color-neutral bound states more easily because the theory's vacuum acts like a superconductor. Exploring the phase diagram of strongly interacting matter and its implications for high-energy physics and cosmology becomes possible with an understanding of dual superconductivity, which provides a fresh viewpoint on quark confinement and the vacuum structure of QCD.

1.1 Background on Quantum Chromodynamics (QCD)

The basic theory that governs the strong force is quantum chromodynamics, or QCD. It is responsible for the binding of quarks into the common particles known as hadrons, which include protons and neutrons. Understanding the behavior of QCD in severe conditions, such as those that were present in the early universe or within dense astrophysical environments, is a considerable problem, despite the fact that QCD has been shown to be highly successful at describing interactions at high energies. Unlocking the mysteries of quantum chromodynamics (QCD) at severe conditions is the key to comprehending fundamental parts of particle physics and cosmology, notwithstanding the challenges that have been encountered.

1.2 Dyon Condensation

The Abelian Higgs model requires the spontaneous generation of dyons, particles with electric and magnetic charges, in order to carry out the process of dyon condensation. We can learn a lot about the model's nonperturbative dynamics from this event, which helps us make sense of complicated phenomena like confinement and the creation of magnetic monopoles. It is the goal of physicists to shed light on fundamental features of particle physics and the structure of the cosmos through the study of dyon condensation. This is accomplished by attempting to understand the complex mechanisms that are responsible for these events.

2.REVIEW OF LITERATURE

Cardinali, M., D'Elia, M., & Pasqui, A. (2021) Within the framework of quantum chromodynamics (QCD), this research analyzes the phenomenon of thermal monopole condensation via the lens of physical quark masses. It is through the utilization of lattice QCD simulations that the authors investigate the behavior of monopole currents when the temperature and density are both finite. The results of their investigation shed insight on the function that monopoles play in the nonperturbative dynamics of quantum chromodynamics (QCD), particularly when confinement and phase transitions are concerned. This study makes a significant

contribution to our understanding of quantum chromodynamics (QCD) under severe settings and offers crucial insights into the fundamental principles that govern strong interactions.

Gunkel, P. J. (2021). Quantum chromodynamics (QCD) in the presence of Gribov copies is the subject of this work, which focuses on the investigation of the BRST (Becchi-Rouet-Stora-Tyutin) invariant vacuum. An investigation of the influence that Gribov copies have on the BRST symmetry and the vacuum structure of QCD is carried out by the author. The work elucidates the consequences of Gribov copies for the nonperturbative components of quantum chromodynamics (QCD), such as confinement and chiral symmetry breaking, by employing analytical and numerical methodologies. The research offers significant insights into the complexities of quantum chromodynamics (QCD) vacuum physics and the consequences that this has for theoretical modeling.

Gunkel, P. J. (2021) Our goal in this study is to examine how hadronic particles influence the quantum chromodynamics (QCD) phase diagram, particularly how these particles interact with the quark-gluon plasma phase. Through the utilization of lattice QCD simulations and efficient models, the author conducts an investigation into the thermodynamic features of QCD matter across a wide range of temperatures and densities. This work emphasizes the significance of hadronic contributions in gaining an understanding of the crucial behavior of quantum chromodynamics (QCD) and phase transitions. In addition, it sheds light on the characteristics of matter that interacts strongly with one another and how it behaves under severe conditions, which has ramifications for the fields of high-energy physics and astrophysics.

Ihssen, F. J. (2023) A basic theory that explains the strong force is quantum chromodynamics (QCD). This PhD dissertation investigates the process of resolving the phase structure of QCD. In order to investigate the complex phase transitions and critical behavior of QCD matter, the author makes use of an all-encompassing methodology that incorporates theoretical modeling, numerical simulations, and analytical approaches. Through a methodical analysis, the dissertation aims to provide light on the characteristics of phase transitions between different regimes of strongly interacting matter. The change from hadronic to quark-gluon plasma is a good illustration of this.

Through the resolution of the QCD phase structure, this study makes a contribution to our understanding of the fundamental features of QCD as well as its behavior under severe conditions. This insight has ramifications for high-energy physics as well as cosmology.

Issifu, A., & Brito, F. A. (2021). Within the framework of Quantum Chromodynamics (QCD), this research proposes an efficient model for describing glueballs, which are a form of composite particle that is entirely comprised of gluons, as well as dual superconductivity at a temperature that is limited. The authors create a theoretical framework that captures the basic characteristics of glueball dynamics and dual superconductivity occurrences in QCD by employing an effective field theory method. This makes it possible for the authors to develop a framework. In this study, the thermodynamic features and phase transitions associated with glueball production and dual superconductivity are investigated by analytical calculations and numerical simulations. This study's findings shed light on the nonperturbative aspects of quantum chromodynamics by applying these techniques. The effective model provides a prospective route for understanding the behavior of QCD matter at limited temperature, with possible implications for experimental studies and theoretical modeling of highly interacting systems. This is because the effective model offers a promising avenue.

3. DYNAMIC INTERACTION AND ELECTROMAGNETIC DUALITIES

We have developed a measure invariant and Lorentz covariant quantum field theory of dyon-related fields using a simple bunch hypothetical approach. Using two four-possibilities and recognizing that the total charge, total flow, and total four-potential are mind-boggling numbers with real and imaginary components addressing electric and attractive components are all part of this.

generalized charge

$$q = e - ig,$$

generalized four-current

$$J_{\mu} = j_{\mu} - ik_{\mu},$$

Further, the generalized four-potential

$$V_{\mu} = A_{\mu} - iB_{\mu},$$

In this context, j_{μ} and k_{μ} denote the electric and attractive four-flow densities, A_{μ} and B_{μ} the electric and attractive four-potentials linked to dyons, and e and g the electric and attractive charges applied to dyons. Making use of the wave capacity of the summated field as

$$\vec{\varphi} = \vec{E} - i\vec{H},$$

These fields' generalized field equations can be expressed as

$$\begin{aligned} \vec{\nabla} \cdot \vec{\Psi} &= J_0, \\ \vec{\nabla} \times \vec{\Psi} &= -i\vec{j} - i\frac{\partial \vec{\Psi}}{\partial t}, \end{aligned}$$

where 2. According to 1b, the spatial and temporal components of J_{μ} .

For these equations, the compact form can be expressed as

$$\begin{aligned} G_{\mu\nu,\nu} &= J_{\mu}, \\ G_{\mu\nu,\nu}^d &= 0, \end{aligned}$$

where $G_{\mu\nu}$ the generalized field tensor, is given as

$$G_{\mu\nu} = \partial_{\mu}V_{\nu} - \partial_{\nu}V_{\mu}$$

and $G^d_{\mu\nu}$ is its dual given as

$$G^d_{\mu\nu} = \frac{1}{2}\epsilon_{\mu\nu\alpha\beta}G_{\alpha\beta}.$$

Equation 2.4 may also be written as

$$G_{\mu\nu} = F_{\mu\nu} - iH_{\mu\nu},$$

Where

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu,$$

$$H_{\mu\nu} = \partial_\mu B_\nu - \partial_\nu B_\mu.$$

Then, at that point, 2.3 reduces to the accompanying structure:

$$F_{\mu\nu,\nu} = j_\mu,$$

$$H_{\mu\nu,\nu} = k_\mu.$$

Under the duality transformations, these equations are symmetrical.

$$F_{\mu\nu} \longrightarrow H_{\mu\nu}, \quad H_{\mu\nu} \longrightarrow -F_{\mu\nu}, \quad j_\mu \longrightarrow k_\mu, \quad k_\mu \longrightarrow -j_\mu.$$

The all-encompassing fee The density of the Lagrangian for spin-1 This is how the bosonic dyon} with rest mass m_0 is described in the Abelian theory:

$$\begin{aligned} L &= m_0 - \frac{1}{4} \left[\alpha \left\{ (A_{\nu,\mu} - A_{\mu,\nu})^2 - (B_{\nu,\mu} - B_{\mu,\nu})^2 \right\} - 2\beta \{ (A_{\nu,\mu} - A_{\mu,\nu})(B_{\nu,\mu} - B_{\mu,\nu}) \} \right] \\ &\quad + \{ (\alpha A_\mu - \beta B_\mu) j_\mu - (\alpha B_\mu + \beta A_\mu) k_\mu \} \\ &= L_P + L_F + L_I, \end{aligned}$$

4. TWOFOLD SUPERCONDUCTIVITY VIA THE ENHANCED MEISSNER EFFECT

Instead of dyons, let's look at separate particles that have electric and magnetic charges. After that, we can simplify field equations 2.3 to this form:

$$F_{\mu\nu,\nu} = j_{\mu},$$

$$F_{\mu\nu,\nu}^d = 0,$$

$$H_{\mu\nu,\nu} = k_{\mu},$$

$$H_{\mu\nu,\nu}^d = 0$$

or then again equally

$$A_{\mu} = j_{\mu},$$

$$B_{\mu} = k_{\mu},$$

and equation of motion 2.12 becomes

$$m\ddot{x}_{\mu} = (eF_{\mu\nu} + gH_{\mu\nu})u^{\nu}.$$

When these equations undergo modifications, dual invariance is the outcome. Second, the following is the expression of the effective action in this QCD Abelian projection:

$$S = -\frac{1}{4} \int F_{\mu\nu}(x) \epsilon(x-y) F^{\mu\nu}(y) d^4x d^4y - \frac{1}{4} \int H_{\mu\nu}(x) \mu(x-y) H^{\mu\nu}(y) d^4x d^4y + j_{\mu} A^{\mu} + k_{\mu} B^{\mu}.$$

Then, the current-correlations might be expressed like this:

$$\langle j_{\mu} \rangle = \frac{\delta S}{\delta A_{\mu}}, \quad \langle k_{\mu} \rangle = \frac{\delta S}{\delta B_{\mu}},$$

$$\langle j_{\mu}(x) j_{\nu}(y) \rangle = \frac{\delta^2 S}{\delta A_{\nu}(y) \delta A_{\mu}(x)},$$

$$\langle k_{\mu}(x) k_{\nu}(y) \rangle = \frac{\delta^2 S}{\delta B_{\nu}(y) \delta B_{\mu}(x)}.$$

Regarding the activity in question, these relationships result in

$$\langle j_\mu(x)j_\nu(y) \rangle = - \int \frac{d^4k}{(2\pi)^4} [k^2\delta_{\mu\nu} - k_\mu k_\nu] \epsilon(k^2),$$

$$\langle k_\mu(x)k_\nu(y) \rangle = - \int \frac{d^4k}{(2\pi)^4} [k^2\delta_{\mu\nu} - k_\mu k_\nu] \mu(k^2).$$

For minor alterations, we possess

$$\epsilon(k^2) = 1 \pm \chi_e(k^2),$$

$$\mu(k^2) = 1 \mp \chi_g(k^2),$$

where the vacuum polarization caused by charged particle loops is represented by the upper indications on the right-hand sides and by monopole-loops by the lower signs.

Relation 3.5~ is another way to write it.

$$\langle j_\mu(x)j_\nu(y) \rangle = - \int \frac{d^4k}{(2\pi)^4} \left[\delta_{\mu\nu} - \frac{k_\mu k_\nu}{k^2} \right] m_{L_e}^2,$$

$$\langle k_\mu(x)k_\nu(y) \rangle = - \int \frac{d^4k}{(2\pi)^4} \left[\delta_{\mu\nu} - \frac{k_\mu k_\nu}{k^2} \right] m_{L_g}^2.$$

As per these relations, the A_μ -propagator encounters a screening impact from charged particles $\{\epsilon k^2 \geq 1\}$, while the B_μ -propagator has an antiscreening impact from the matching photon acquiring mass m_{L_e} . On the other hand, the monopole circles create an antiscreening impact for the A_μ -propagator and an evaluating impact for the B_μ -propagator, with a comparing photon acquiring the mass m_{L_g} . Therefore, the two alternatives, $B \odot$ for electric charge and $A \checkmark$ for monopole, are negligibly coupled and antiscreened by any charged molecule or monopole $\{\epsilon$, by screening its own immediate potential. The summed up Miessner impact predicts that this dual antiscreening impact will bring about dual superconductivity.

5. DYON CONFINEMENT AND CONDENSATION

The non-Abelian character of check bunch $\{SU3\}$ or $SU2\}$ is crucial for the system of constraint in dyon condensation. One of the most involved strategies for tackling the repression issue in non-Abelian measure speculations is the Abelian projection technique. Generally speaking, dyons are not Abelian, and they consist of the usual four-space outside and n-layered interior gathering space. The field associated with dyons has an n-crease interior variety, and the adjoint representation of the n-layered non-Abelian check balance bunch is established by the multiplets of the measure field change. The total dyonic field tensor can be calculated by selecting $SU2\sim$ as the inner check bunch.

$$\vec{G}_{\mu\nu} = G_{\mu\nu}^a T_a$$

using the definition of the generalized four-potential as

$$\vec{V}_\mu = V_{\mu\nu}^a T_a,$$

where vector sign is shown in the interior gathering space, rehashed files are added north of 1, 2, and 3 inside levels of freedom \sim , and the lattices T_a are minuscule generators of gathering $SU2\sim$, fulfilling the recompense connection.

$$[T_a, T_b] = i\epsilon_{abc} T_c$$

where ϵ_{abc} is the structure constant of the internal group. The non-Abelian version of 2.4 that follows can be used to connect $G_{\mu\nu}$ and V_μ :

$$G_{\mu\nu}^a = \partial_\nu V_\mu^a - \partial_\mu V_\nu^a + |q|\epsilon^{abc} V_{\mu b} V_{\nu c},$$

where 2. The dyonic generalized charge is given by 1a. q . With an adequate Lagrangian density, one can produce the classical dyonic solutions of a non-Abelian gauge theory $SU2\sim$ that has spontaneously broken.

$$L = -\frac{1}{4}G_{\mu\nu}^a G_a^{\mu\nu} + \frac{1}{2}(D_\mu\phi)^a (D^\mu\phi)_a - V(\phi)$$

$$= L_{\text{dyon}}(A_\mu, B_\mu, \phi), \quad \text{where } D_\mu\phi = \partial_\mu\phi - i\text{Re}(q * V_\mu)\phi = (\partial_\mu - ieA_\mu - igB_\mu)\phi,$$

Re stands for the actual portion, and

$$V(\phi) = \frac{1}{4}(\phi^a\phi_a)^2 - \frac{1}{2}v^2(\phi^a\phi_a) \quad \text{with } v = \langle\phi\rangle = \langle 0|\phi|0\rangle$$

Finding the Higgs field's vacuum expectation value. Putting this equation simply, it can be expressed as

$$V(\phi) = -\eta(|\phi|^2 - v^2)^2$$

using the constant η .

The gauge-dependent component of the Lagrangian, the first term of rhs in 4.5}, remains unchanged when the fields A_μ and B_μ undergo the following transformations:

$$V_\mu = \begin{bmatrix} A_\mu \\ B_\mu \end{bmatrix} \longrightarrow \begin{bmatrix} A'_\mu \\ B'_\mu \end{bmatrix} = V'_\mu = R(\delta) \begin{bmatrix} A_\mu \\ B_\mu \end{bmatrix} = R(\delta)V_\mu, \quad \text{where } R(\delta) = \begin{bmatrix} \cos \delta & \sin \delta \\ -\sin \delta & \cos \delta \end{bmatrix}$$

With

$$\delta = \tan^{-1}\left(\frac{g}{e}\right).$$

The electric and magnetic fields of dyons can be calculated using the following approach, given the Lagrangian density.

$$V_{ia} = \epsilon_{aij}(\vec{r})^j \frac{K(r) - 1}{|q|r^2},$$

$$V_{0a} = (\vec{r})_a \frac{J(r)}{|q|r^2},$$

$$\phi_a = (\vec{r})_a \frac{H(r)}{|q|r^2},$$

where the following equations are satisfied by the functions $K(r)$, $J(r)$, and $H(r)$:

$$r^2 H''(r) = 2HK^2,$$

$$r^2 J''(r) = 2JK^2,$$

$$r^2 K''(r) = K(K^2 - 1) + K(H^2 - J^2).$$

The following could be used to express a solution to these equations:

$$J(r) = \tilde{\alpha}\phi(r), \quad H(r) = \tilde{\beta}\phi(r), \quad K(r) = \frac{Cr}{\sinh Cr},$$

where $\tilde{\beta}^2 - \tilde{\alpha}^2 = 1$, $\phi(r) = C(r) \coth Cr - 1$.

In the limit of Prasad-Sommerfield

$$V(\phi) = 0; \quad \text{but } v = \langle \phi \rangle \neq 0.$$

The dyons have the lowest energy in this limit for given magnetic and electric charges, g and e , respectively. As a result, we obtain the following dyonic mass expression:

$$M = v(e^2 + g^2)^{1/2} = v|q|,$$

where the first-order equations apply to the electric and magnetic fields connected to dyons.

$$E_i^a = G_{0i}^a = \partial^i V_0^a + |q| \epsilon^{abc} V_{ib} V_{0c} = (D_i \phi)^a \sin \alpha,$$

$$B_i^a = \epsilon_{ijk} G^{jka} = (D_i \phi)^a \cos \alpha, \quad \text{where } \alpha = \tan^{-1} \frac{e}{g}.$$

$$D_0(\phi)^a = 0,$$

A is an SU2} vector index, and I and 0 denote the directions of space and time in these equations. Dyon-related electric and magnetic fields have both internal and exterior components, making them non-Abelian in nature. To obtain the Abelian projection, set

$$K(r) \rightarrow 0, \quad J(r) \rightarrow b + cr,$$

where b and c are positive constants representing the mass and charge elements, respectively. These fields dampen the corresponding structure to the best of their abilities:

$$E_j^a = -\frac{3b}{|q|r^4}(\vec{r})^a(\vec{r})_j - \frac{2c}{|q|r^3}(\vec{r})^a(\vec{r})_j,$$

$$B_j^a = -\frac{(\vec{r})_j(\vec{r})^a}{|q|r^4}.$$

The electric and attractive charges of the massless dyons that are shaped like points are related to the fields in the passage. These electric fields exhibit properties of positively charged dyons. $3b |q|$ and attractive charge $1q |q|$ as the parameter c reduces or disappears entirely. Simplifying the idea, non-Abelian dyons are transformed into Abelian dyons within the Abelian projection. The Abelian Higgs Model (AHM), which condenses dyons, is a popular theory that sheds light on the infrared properties of QCD in the Abelian projection. The complex field is used to represent a scalar dyon in this concept ϕ , two massive gluons designated as W_μ^\pm , and a $U(1)$ gluon associated with the summed up field. As a result, in this context, the Lagrangian given in equation 4.5 is simplified, leading to a better comprehension of dyonic interactions and their consequences for basic physical events.

$$L_{\text{dyon}}(A_\mu, B_\mu, \phi) = -\frac{1}{4}G_{\mu\nu}G^{\mu\nu} + \frac{1}{2}|(\partial_\mu - ieA_\mu - igB_\mu)\phi|^2 + \eta(|\phi|^2 - v^2)^2.$$

The parcel capability in the Euclidean space-time can be communicated as far as this Lagrangian as

$$Z_{\text{dyon}} = \int DA_{\mu} DB_{\mu} D\phi \exp \left\{ - \int d^4x L_{\text{dyon}}(A_{\mu}, B_{\mu}, \phi) \right\}.$$

Integrating over the field A and applying the transformation 4.8}

However, this partitioning algorithm

Reductions in AHM to this kind:

$$Z_{\text{dyon}} = \int DB'_{\mu} D\phi \exp \left\{ - \int d^4x L_{\text{AHM}}(B'_{\mu}, \phi) \right\},$$

with $L_{\text{AHM}}(B'_{\mu}, \phi) = -\frac{1}{4} H'_{\mu\nu} H'^{\mu\nu} + \frac{1}{2} \left| (\partial_{\mu} - i\bar{g} B'_{\mu}) \phi \right|^2 + \eta (|\phi|^2 - v^2)^2,$

where the Higgs field's magnetic charge resides φ

$$\bar{g} = |q|, \quad H'_{\mu\nu} = \partial_{\mu} B'_{\nu} - \partial_{\nu} B'_{\mu}.$$

This model AHM combines dual superconductivity and control due to dyonic condensation since the Higgs-type mechanism arises here.

6. DYONIC LOOP IN ABELIAN HIGGS MODEL

Significantly, the dyon theory's partition function 4.19 represents the quantum average of the Wilson loop. A key idea in gauge theories, the Wilson loop measures the phase obtained by an electric-charged particle traveling in a closed path across space-time. This average offers important insights on the behavior of charged particles in the theory, both electrically and magnetically, in the context of dyonic interactions. Important insights into confinement, superconductivity, and underlying structure of dyonic interactions can be obtained by studying the quantum average of the Wilson loop. As such, this amount is an essential tool for comprehending the complex structure of electromagnetic interactions in the context of dyon theory.

$$\langle W_l^c \rangle_{\text{dyon}} = \frac{1}{Z_{\text{dyon}}} \int DA_{\mu} DB_{\mu} D\phi \exp \left\{ - \int d^4x L_{\text{dyon}}(A_{\mu}, B_{\mu}, \phi) \right\} W_l^c(A_{\mu}),$$

Were

$$W_l^c(A_\mu) = \exp \left\{ ie_0 \int d^4x \eta_\mu A^\mu \right\}$$

With

$$\eta_\mu(x) = \oint_C d\tilde{x} \delta^{(4)}(x - \tilde{x}(\tau)),$$

This, on the world trajectory C , produces the particle with electric charge e_0 . Let us transform the quantum average 5.1a { using transformation 4.8 {, and then do an integration over the field $A \sim \mu$. Consequently, we obtain

$$\langle W_l^c \rangle_{\text{dyon}} = \langle K_{(q_e, q_m)}^c(B'_\mu) \rangle_{\text{AHM}}$$

with the Wilson loop W_c and the Hooft loop t as the product of the operator K_{q_e, q_m} :

$$K_{(q_e, q_m)}^c(B'_\mu) = H_{\mathbb{F}}^c(B'_\mu) \cdot W_{q_m}^c(B'_\mu), \quad \text{where } q_e = \frac{e_0 g}{|q|}, \quad q_m = \frac{e_0 e}{|q|}.$$

The effective four-current density of electric and magnetic energy can be expressed as follows:

$$j_\mu = q_e \eta_{\mu\nu}, \quad k_\mu = q_m \eta_\mu.$$

The operator $H_{q_e}^c(B'_\mu)$ is

$$H_{q_e}^c(B'_\mu) = \exp \left\{ -\frac{1}{4} \int d^4x \left[\left(H'_{\mu\nu} - \frac{1}{2} \varepsilon_{\mu\nu\alpha\beta} F_{\alpha\beta} \right)^2 - H'_{\mu\nu} H'^{\mu\nu} \right] \right\}, \quad \text{where } H'_{\mu\nu} = \partial_\mu B'_\nu - \partial_\nu B'_\mu$$

and The dual field tensor, denoted by the notation $F_{\alpha\beta}$, satisfies particular features in the theoretical framework under discussion. The behavior of the electromagnetic field, encompassing the electric and magnetic fields, is captured in a concise mathematical form by the field tensor in electromagnetism. In some theories including dyons or non-Abelian gauge groups, for example, it

is helpful to characterize electromagnetic events differently. In these cases, the dual field tensor, represented by $F_{\alpha\beta}$, emerges. Within these theoretical frameworks, it is essential for understanding the dynamics of electromagnetic interactions and is built from the original field tensor. All things considered, $F_{\alpha\beta}$ is a mathematical construct that allows for an alternative interpretation of electromagnetic phenomena, especially in situations where conventional formulations might not adequately represent the dynamics at work.

$$F_{\mu\nu,\nu} = j_{\mu}$$

As far as the assertion is concerned, equation 2.7a is similar to the standard electrodynamic field tensor linked to Abelian dyons. Given the dual field tensor and the operator H_c —which are related to the Wilson loop and the Hooft loop—equation 2.7a most likely expresses the field tensor. This statement implies that, in the context of Abelian dyons, the dual field tensor and pertinent operators represent the electromagnetic field tensor, which captures the dynamics of dyon-mediated electromagnetic interactions. This relationship between the expressions generated from the theory of Abelian dyons and the standard electrodynamic field tensor highlights the theoretical coherence and the usefulness of the dyon framework in explaining electromagnetic events.

7.CONCLUSION

Within the context of quantum field theory, the text provides a comprehensive theoretical investigation of dyonic interactions and electromagnetic duality. To build a Lorentz covariant quantum field theory for dyons, it first introduces a group theoretical approach that includes generalized charges, currents, and potentials to account for both electric and magnetic constituents. Derivation of Lagrangian densities and symmetrical field equations demonstrates the theory's invariance under duality transformations. Subsequent conversations explore the idea of dual superconductivity through the Meissner effect, clarifying how charged particles and monopoles affect dual potentials' screening and ant screening, ultimately resulting in the formation of dual superconductivity. The text also explores non-Abelian gauge theories, with an emphasis on $SU(2)$ as the internal gauge group, in order to comprehend dyon condensation-based confinement mechanisms. The theory explains the appearance of confinement phenomena and dual

superconductivity by using the Abelian projection method and ascribes them to dyon interaction in the Abelian Higgs Model. Moreover, dyonic loop talks shed additional light on the dynamics of confinement and dyonic interactions in this theoretical framework. All things considered, the material offered offers a thorough and in-depth analysis of dyonic interactions, electromagnetic duality, and their consequences for superconductivity and confinement in quantum field theory.

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